

## Math 478/578: Computer Assignment 4 — due Thursday, April 5, 2007

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1. Write a Matlab function `[t,y] = bvpsolve(u,v,w,a,b,alpha,beta,m)` to solve a linear two-point boundary value problem of the form

$$\begin{aligned}y''(t) &= u(t) + v(t)y(t) + w(t)y'(t) \\ y(a) &= \alpha, \quad y(b) = \beta\end{aligned}$$

with the finite difference method. Use the subroutine `tridiag.m` presented in class to solve the tridiagonal linear system.

Assume that the functions  $u$ ,  $v$  and  $w$  are defined separately, e.g., in a driver script.

2. Consider the problem

$$t^2 y''(t) - t(t+2)y'(t) + (t+2)y(t) = 0$$

whose general solution is given by  $y(t) = c_1 t + c_2 t e^t$ .

- (a) What is the solution if the boundary conditions

$$y(1) = e, \quad y(2) = 2e^2$$

are used?

- (b) Test your code from Exercise 1 with this problem. Plot the approximate and exact solutions together for  $m = 19$ .
  - (c) Perform a series of experiments with  $m = 4, 9, 19, 39, 79$ , compute the maximum error and observe how it changes with  $m$  (or  $h$ ).
3. Repeat Exercise 2 for the problem

$$\begin{aligned}y''(t) + 2y'(t) + 10t &= 0 \\ y(0) = 1, \quad y(1) &= 2\end{aligned}$$

whose general solution is given by  $y(t) = -\frac{5}{2}t^2 + \frac{5}{2}t + c_1 e^{-2t} + c_2$ .